

Combining Feature Subsets in Feature Selection

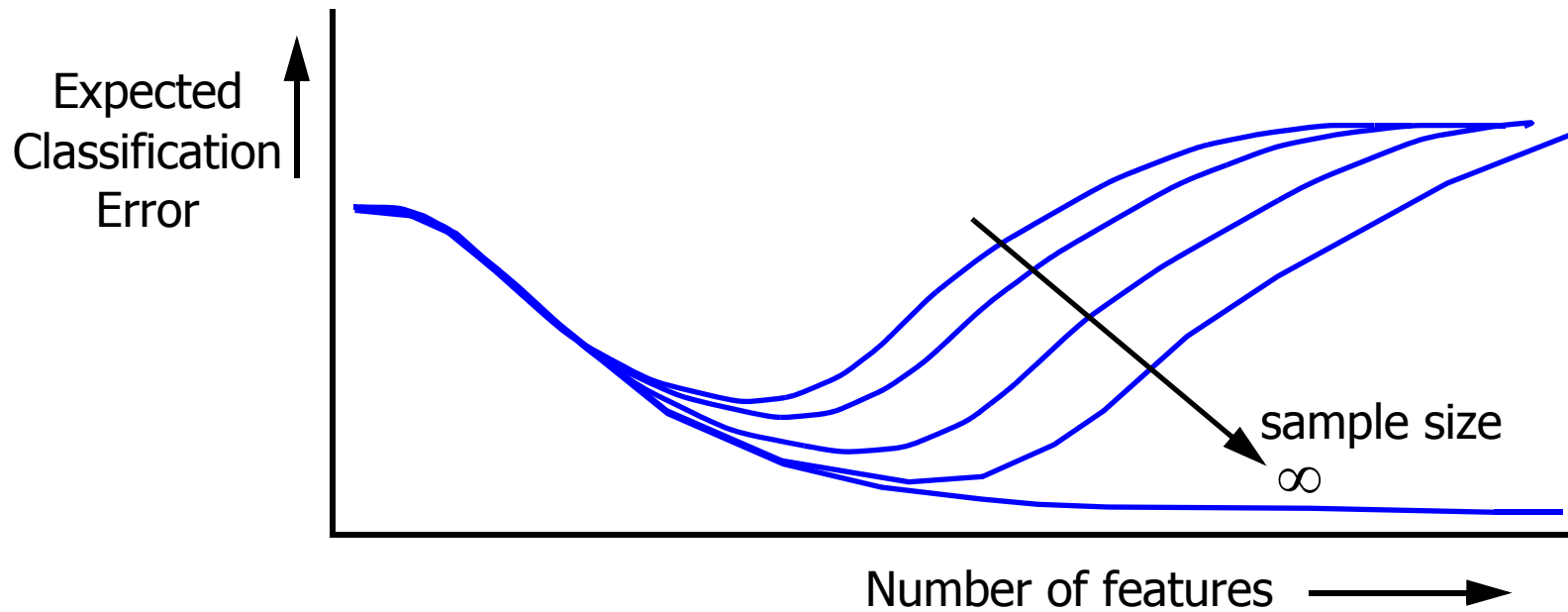
Marina Skurichina, Robert P.W. Duin
June 2005

Delft University of Technology
The Netherlands

Feature Selection

Reasons for feature selection:

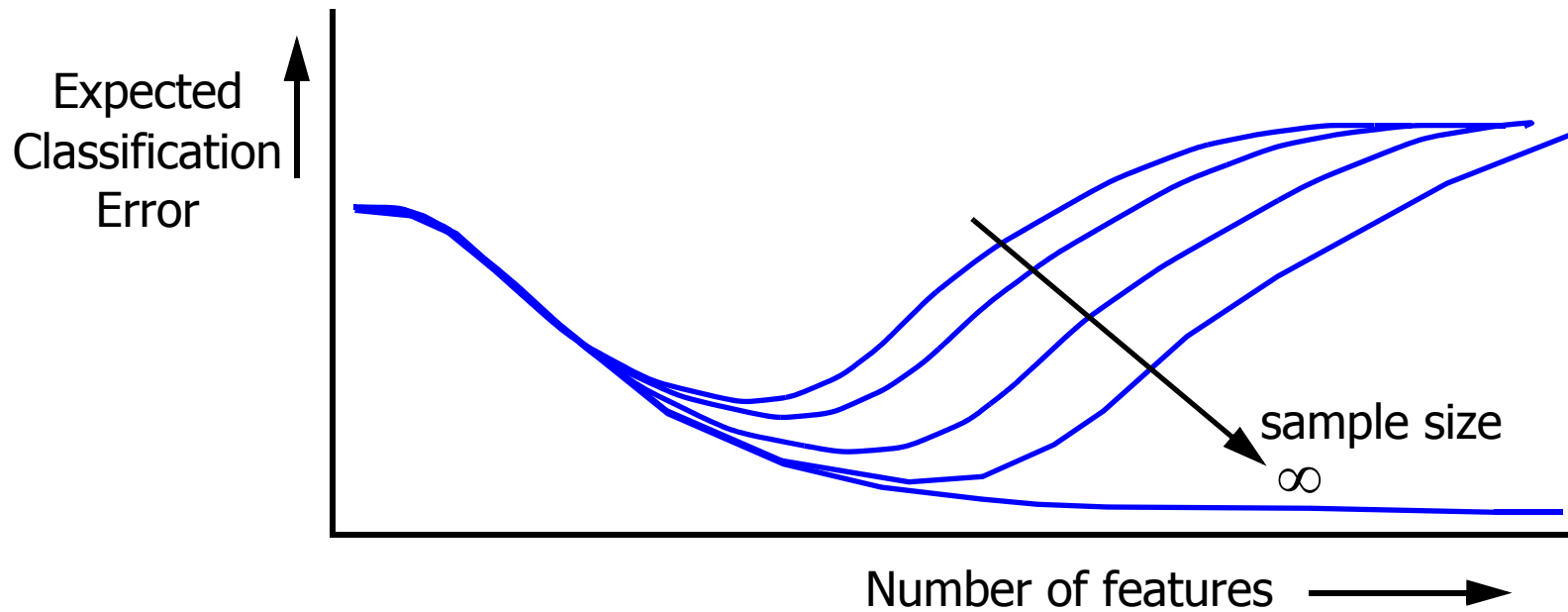
1. Cost reduction: measurements, computations
2. Accuracy



Feature Selection

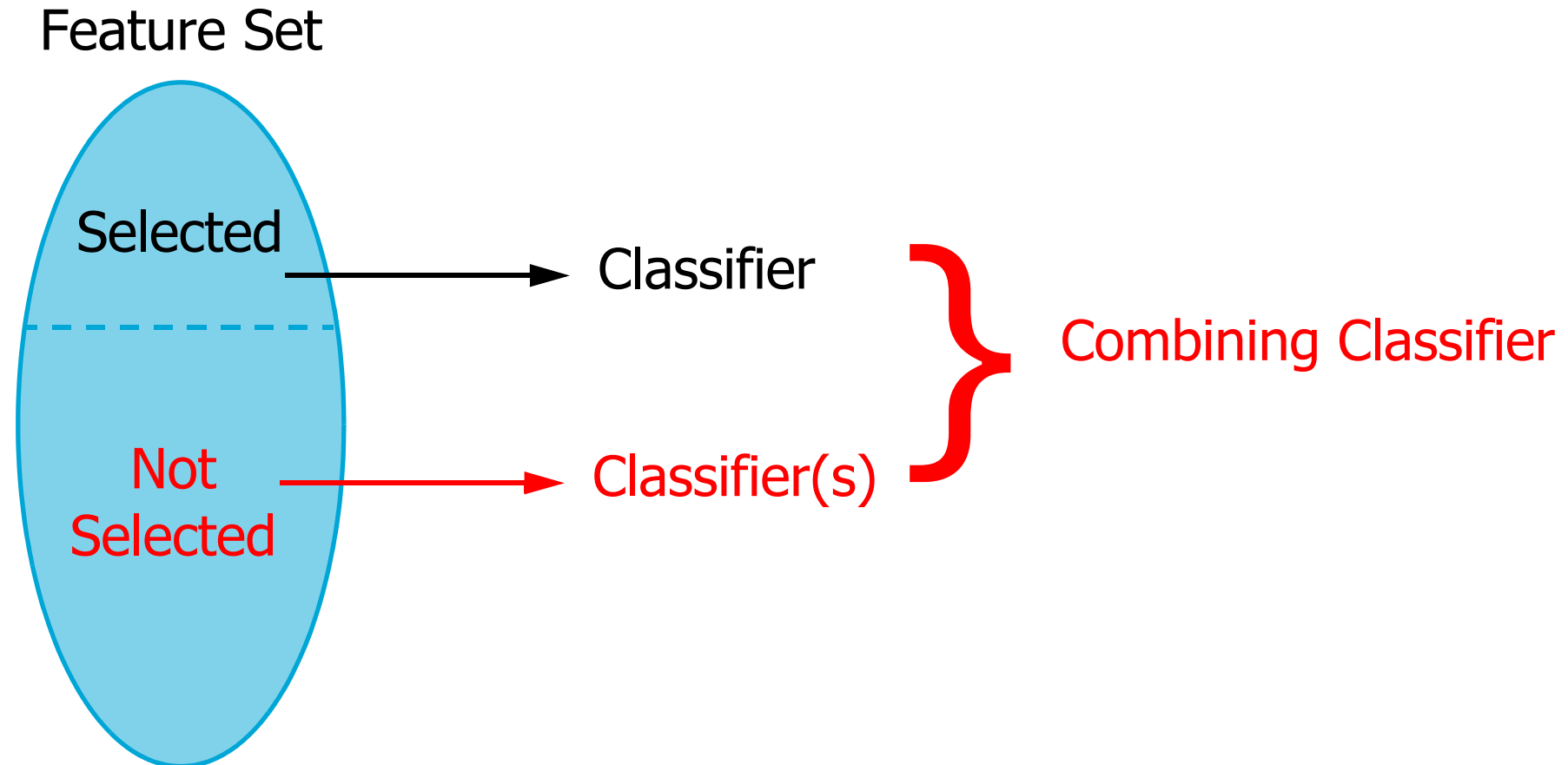
Reasons for feature selection:

1. Cost reduction: measurements, computations
2. Accuracy ?



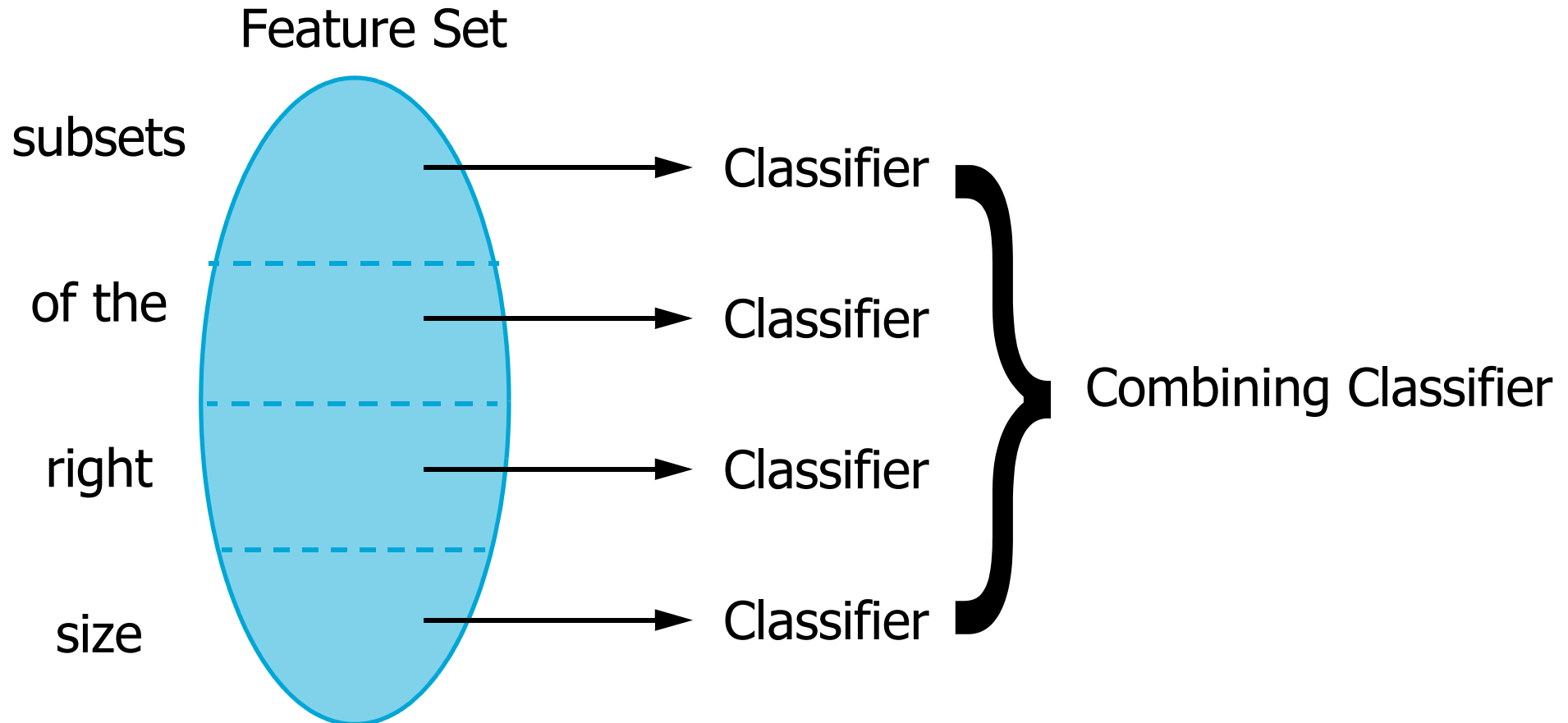
Question 1

Can not-selected features be used to improve classifiers based on the selected features?



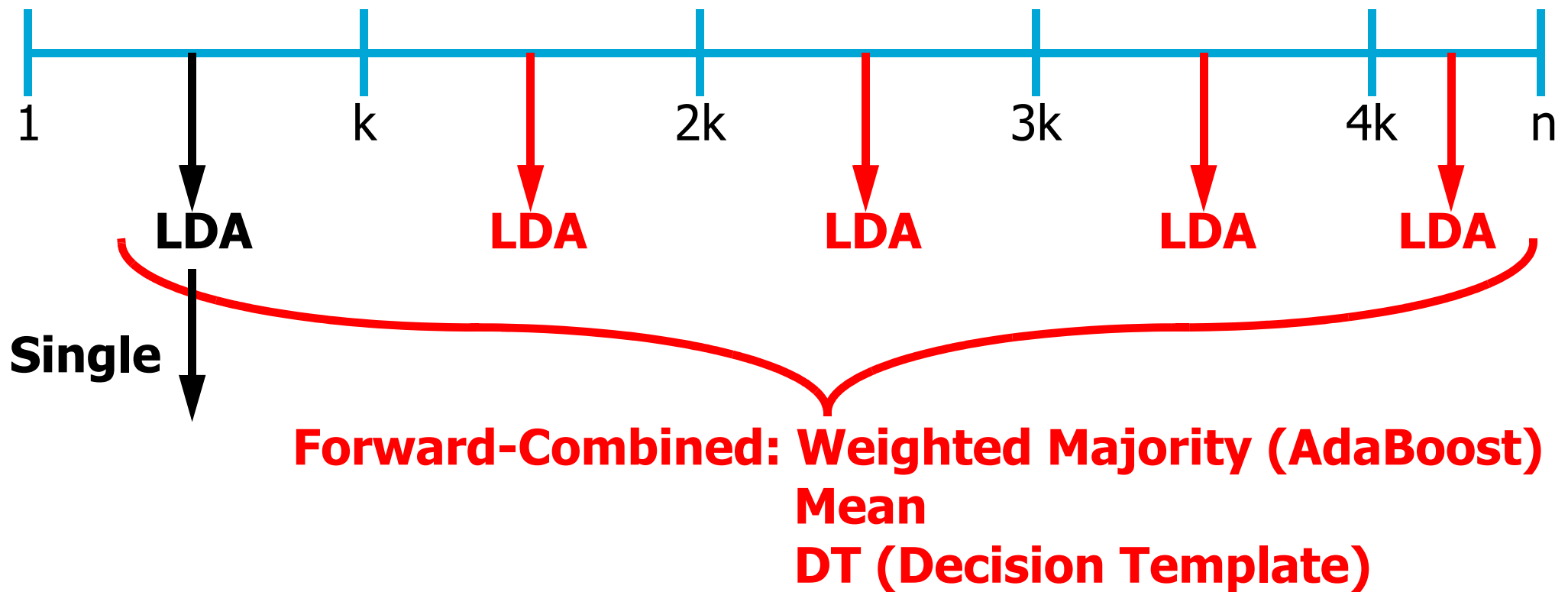
Question 2

Is feature selection needed anyway?



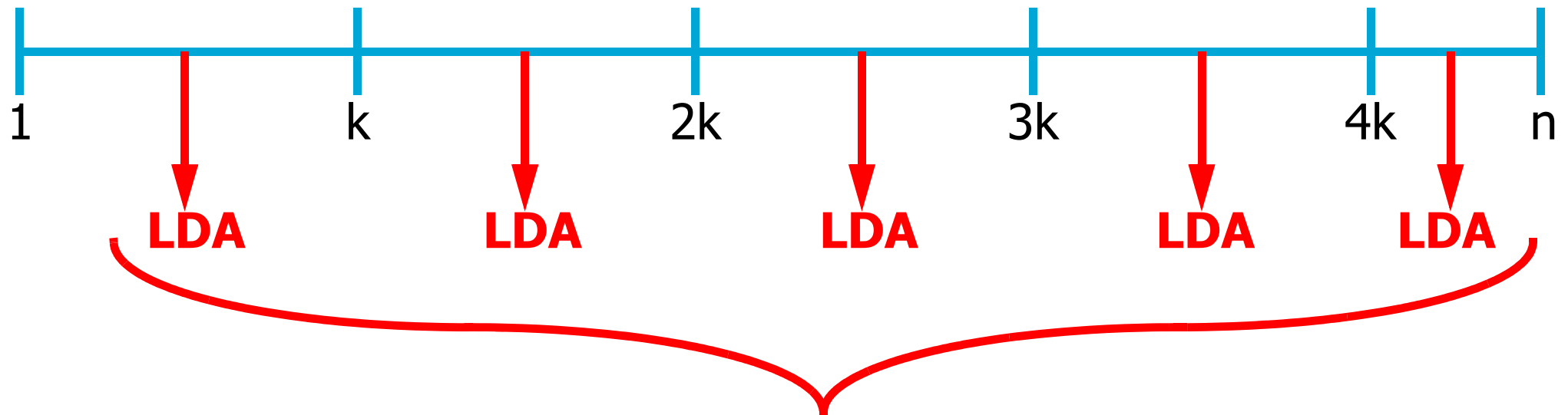
Feature Selection and Ranking

Rank features by forward selection - 1-NN Leave-one-out performance



Random Feature Ranking

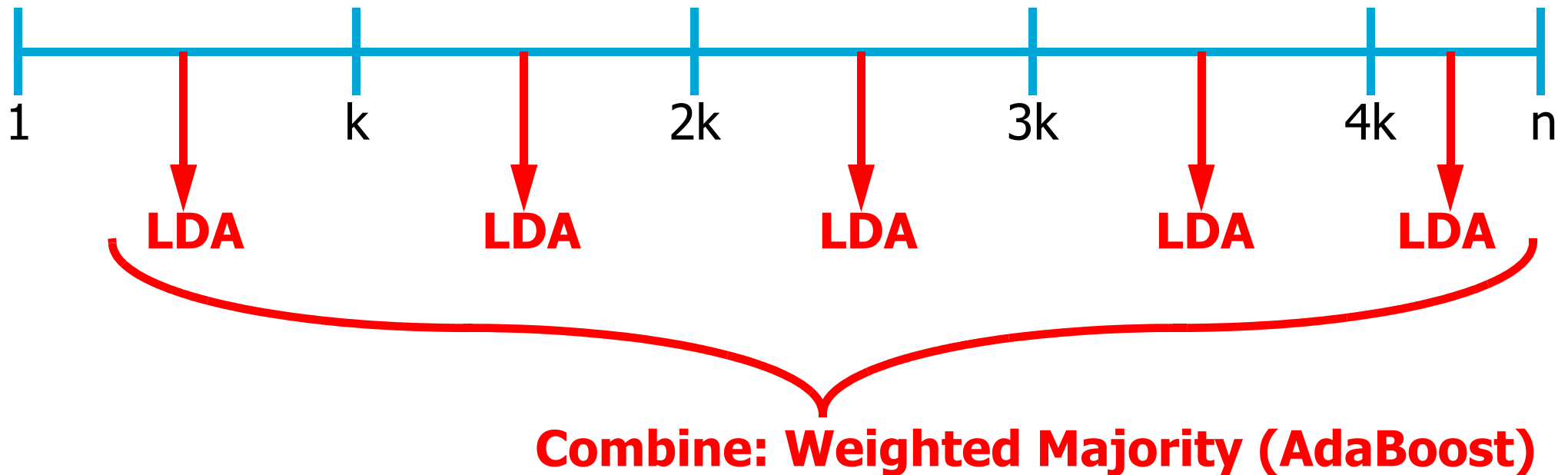
Rank features randomly:



Random Combined: Weighted Majority (AdaBoost)

Random Subspace Method

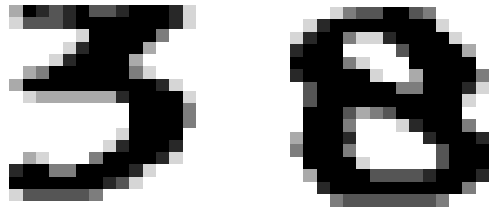
Select repeatedly k out of n features, in total n : doubles and missing!



Experiments

1. Take a dataset.
2. Split at random in train and test set.
3. Rank features.
 - forward selection.
 - random selection (no duplicates, no missings).
 - random subspace (duplicates, missings).
4. Compute for all feature subset sizes (combined) LDA classifiers.
5. Evaluate by test set.
6. Repeat 2-5 50 times, average error estimates.

Experiment 1: NIST Digits

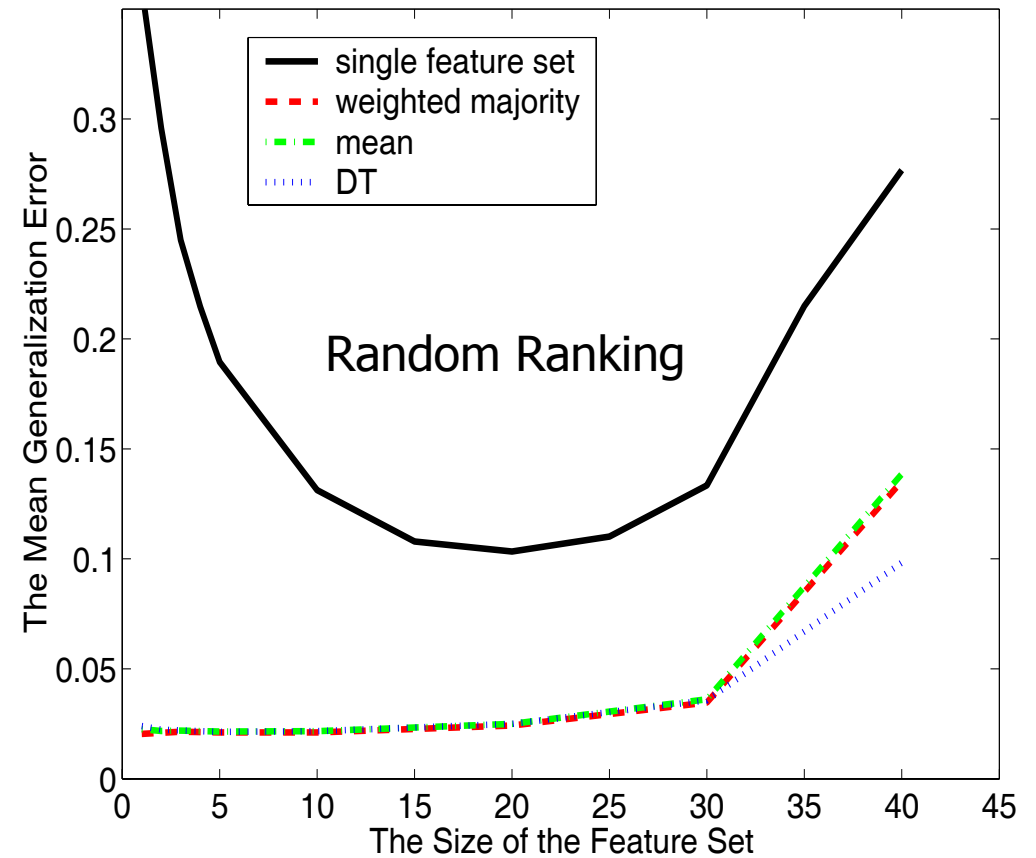
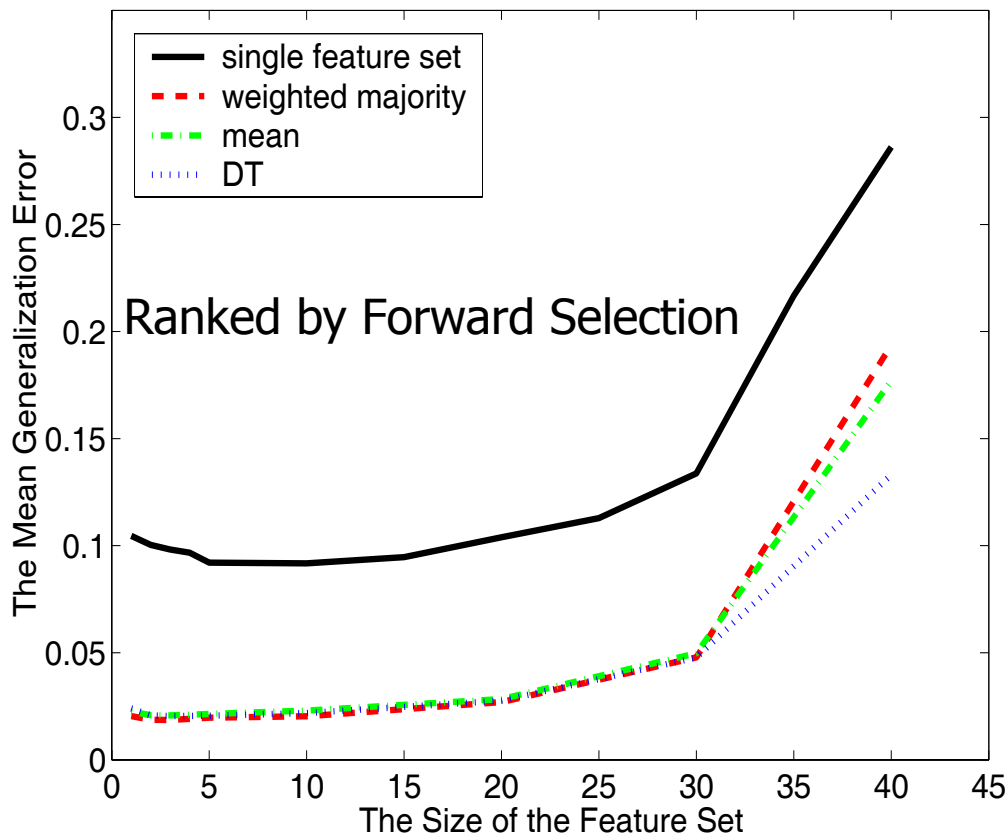


Handwritten Digits 3 and 8

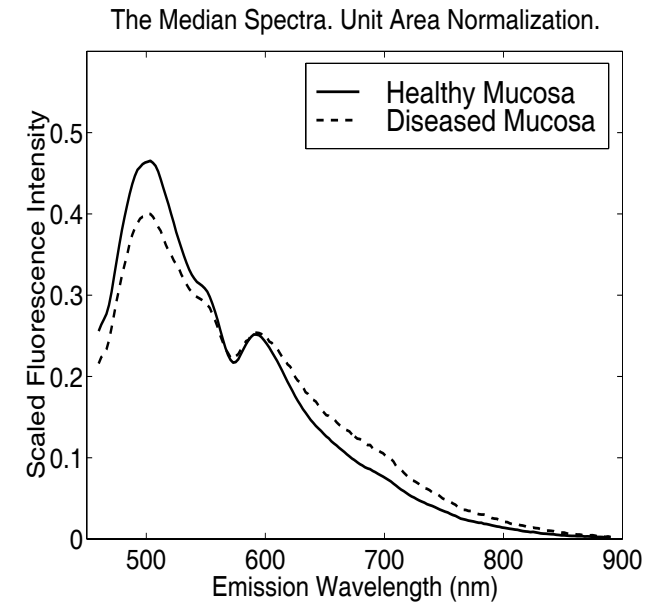
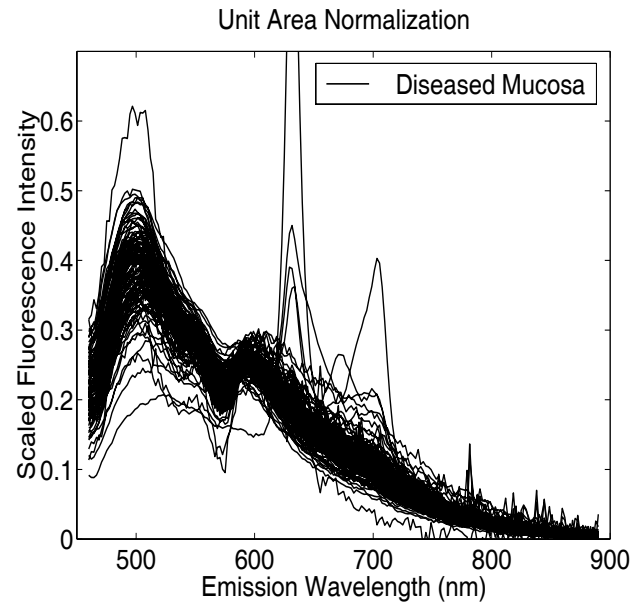
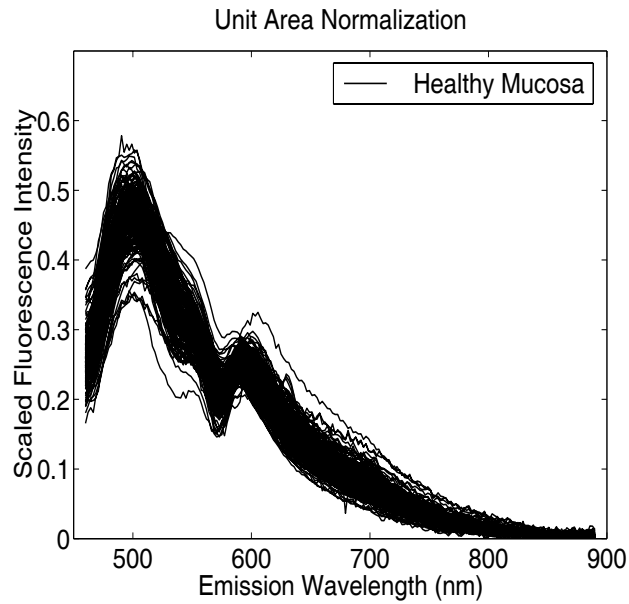
2 x 200 NIST Digits, '3' and '8', 16 x 16 pixels, 256 features.

2 x 100 for training, 2 x 100 for testing

Handwritten Digits 3 and 8



Experiment 2: Spectra

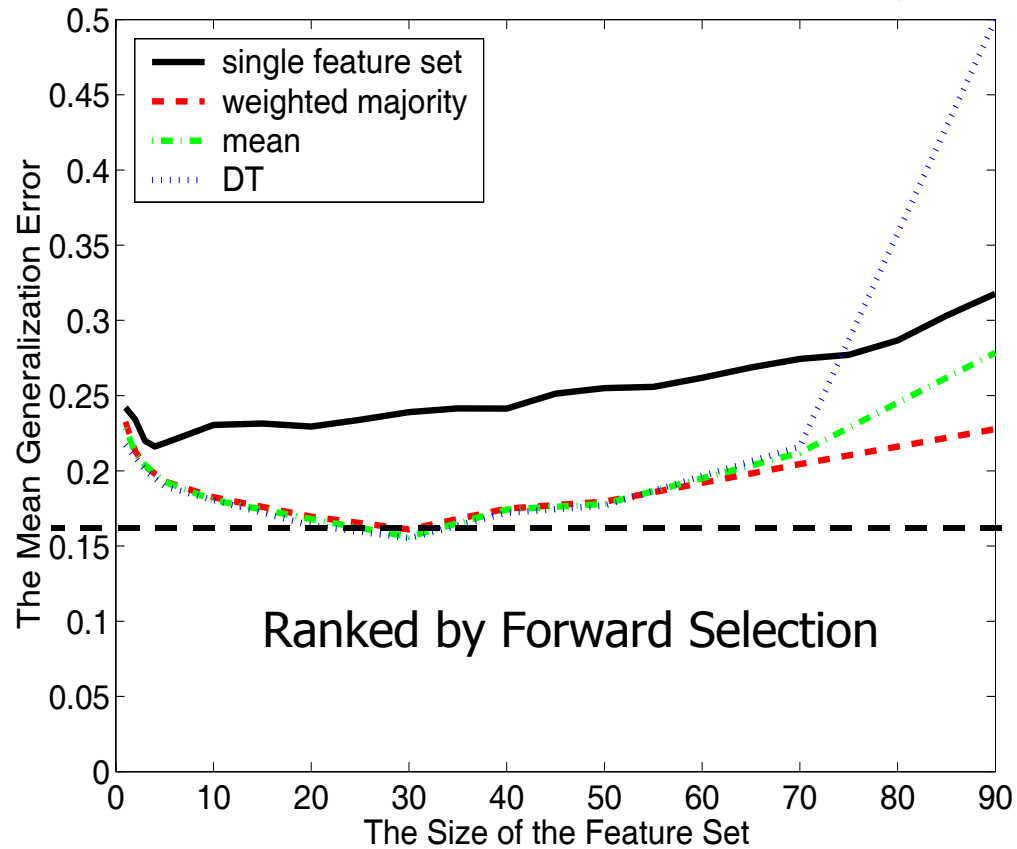


Normalized autofluorescence spectra for healthy and diseased mucosa in oral cavity

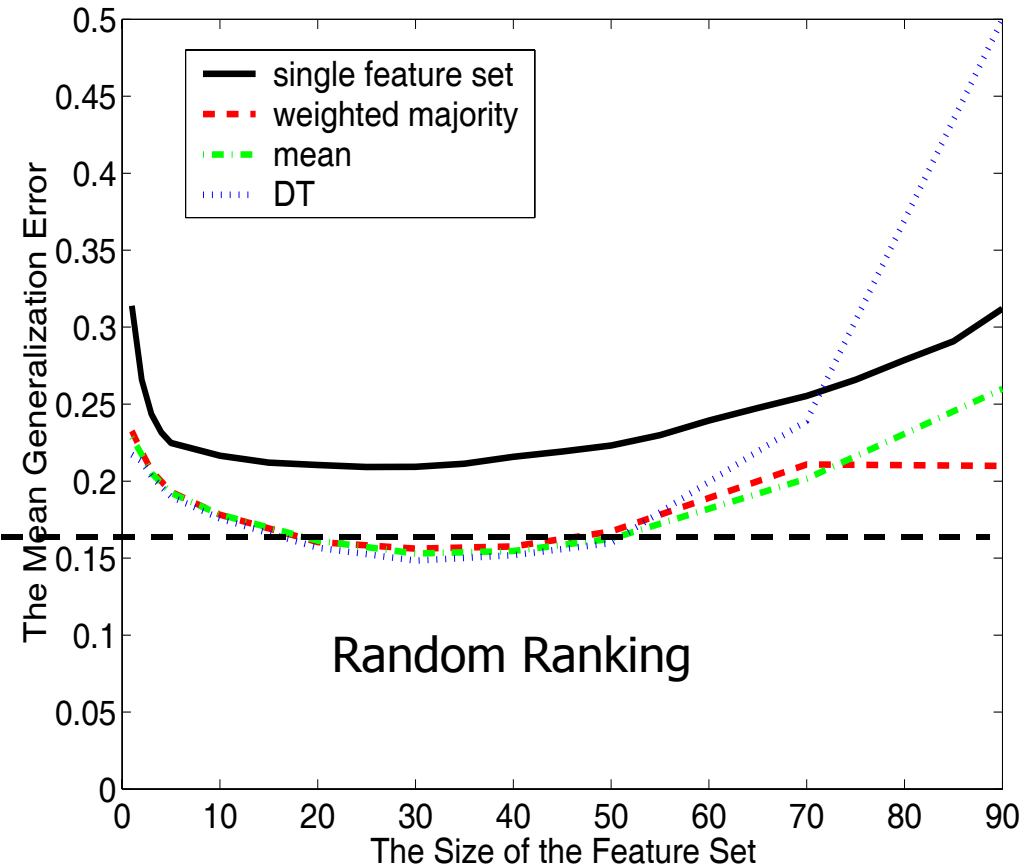
Experiment 2: Results

training set, test set, feature size

Autofluorescence Spectra Measured in Oral Cavity



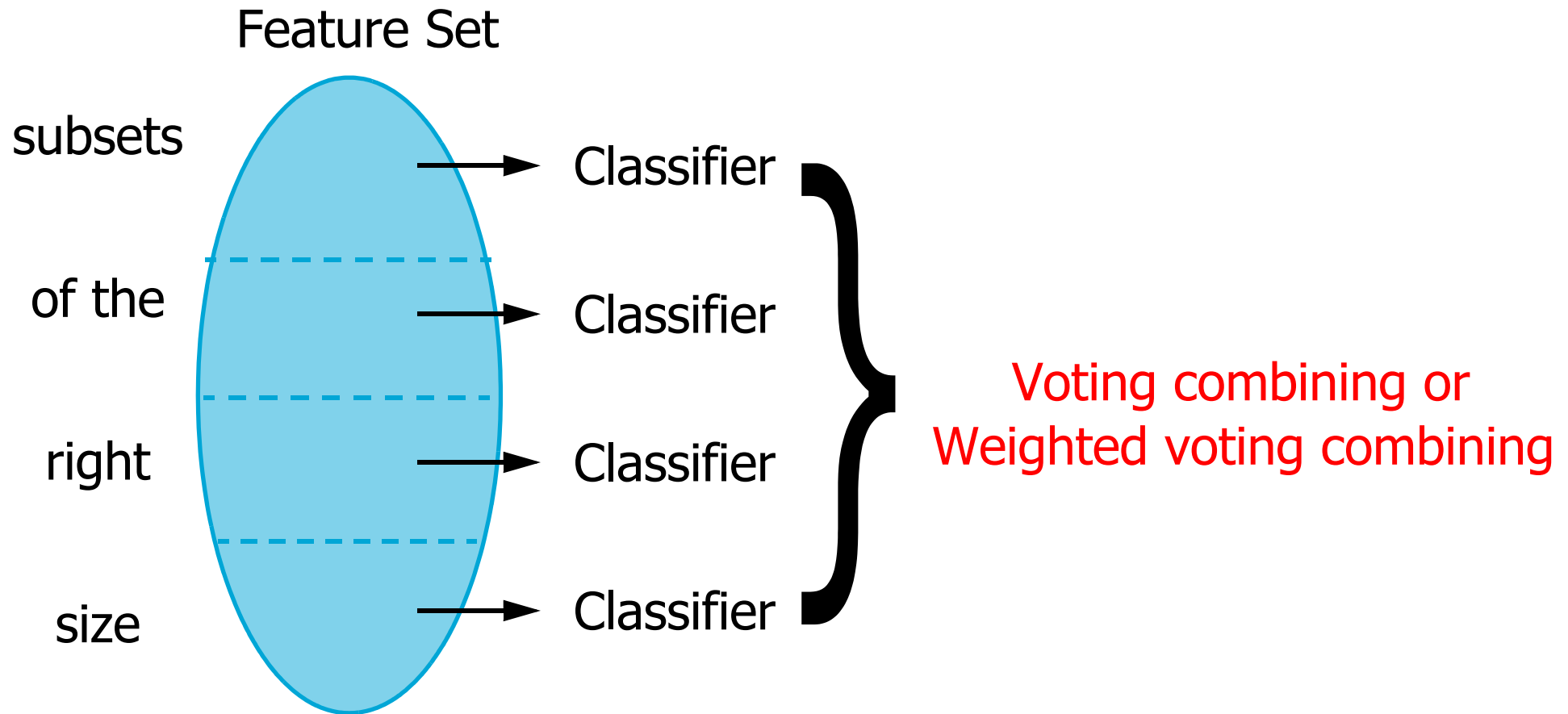
Autofluorescence Spectra Measured in Oral Cavity



Preliminary Conclusions

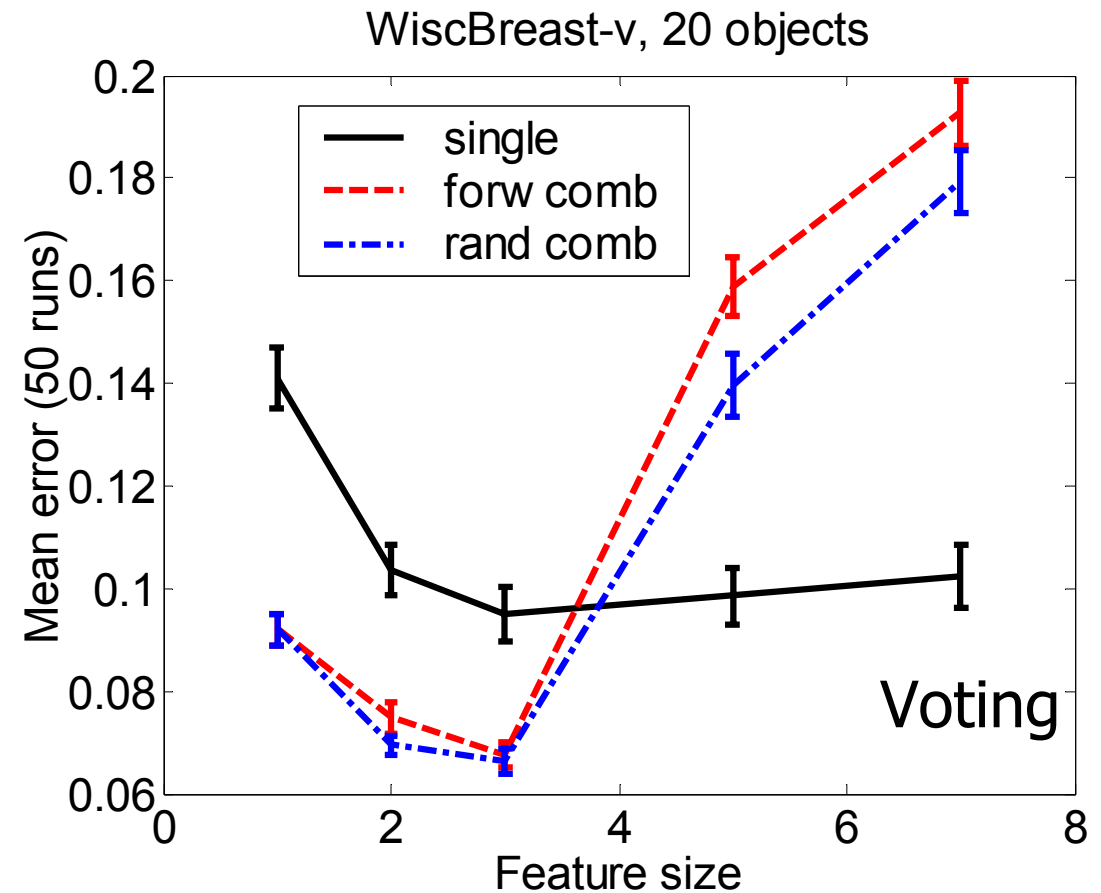
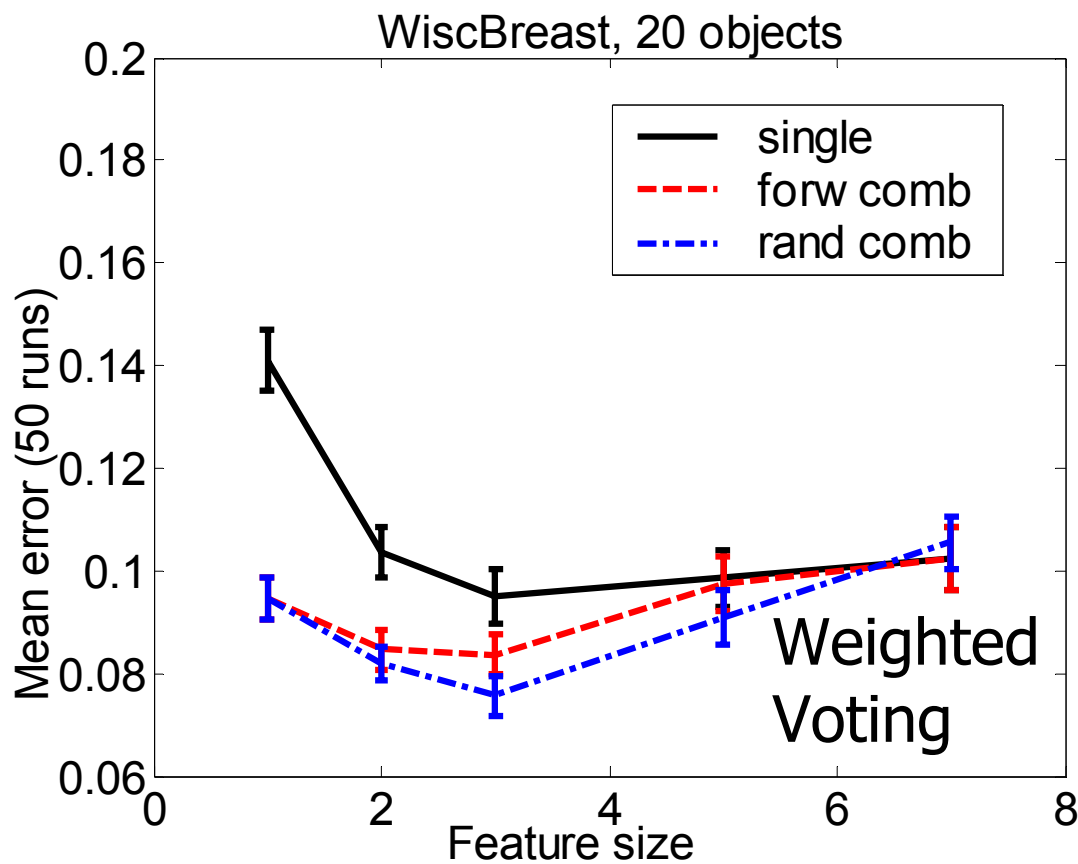
- Subspace combining approach may improve feature selection.
- (Weighted) majority voting seems a good combiner.

Experimental Verification



Ranking according to forward feature selection
or random ranking ?

Wisconsin Breast Cancer Dataset

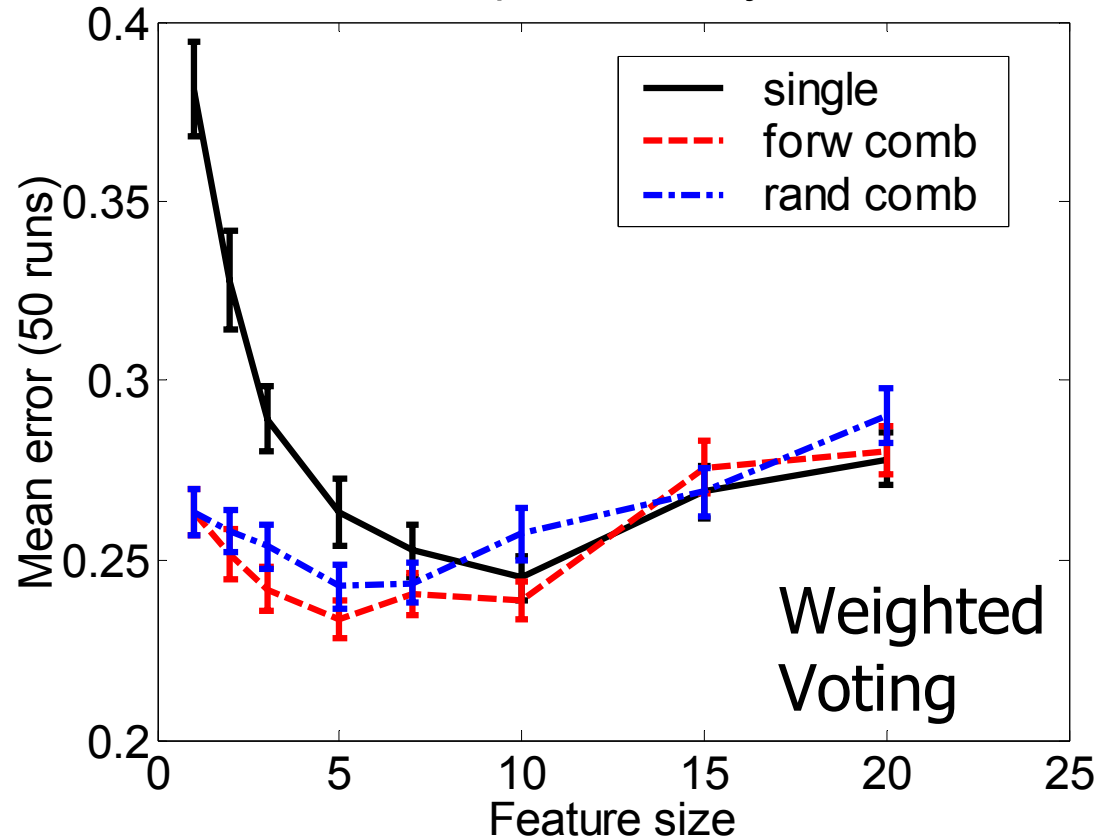


Objects: 683 (444 + 239)

Features: 13

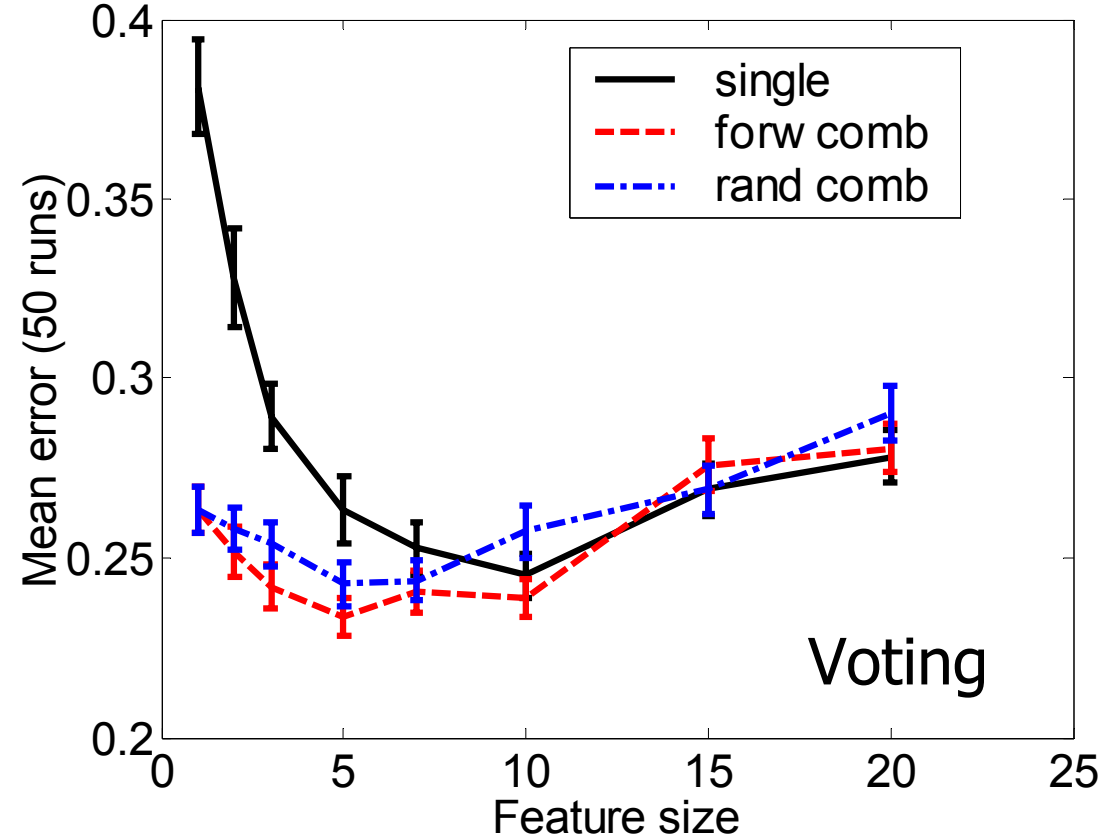
Ionosphere Dataset

Ionosphere, 30 objects



Weighted
Voting

Ionosphere-v, 30 objects

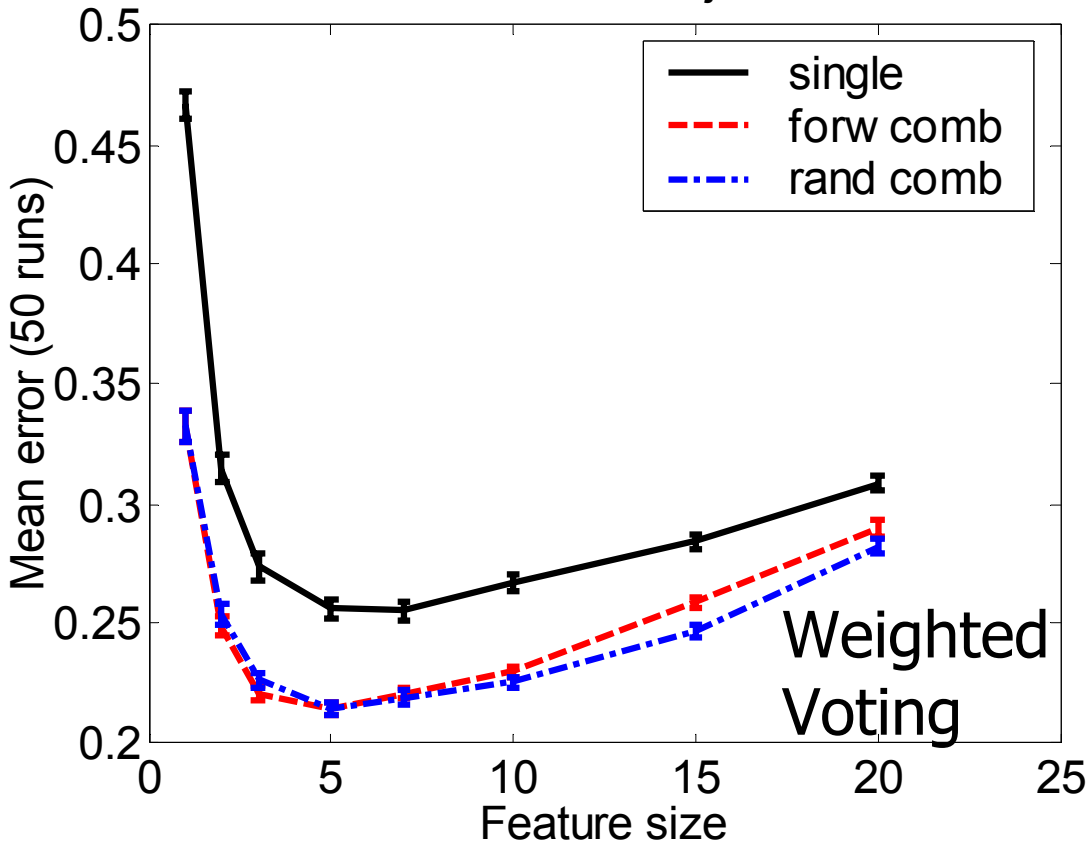


Voting

Objects: 351 (225+126)

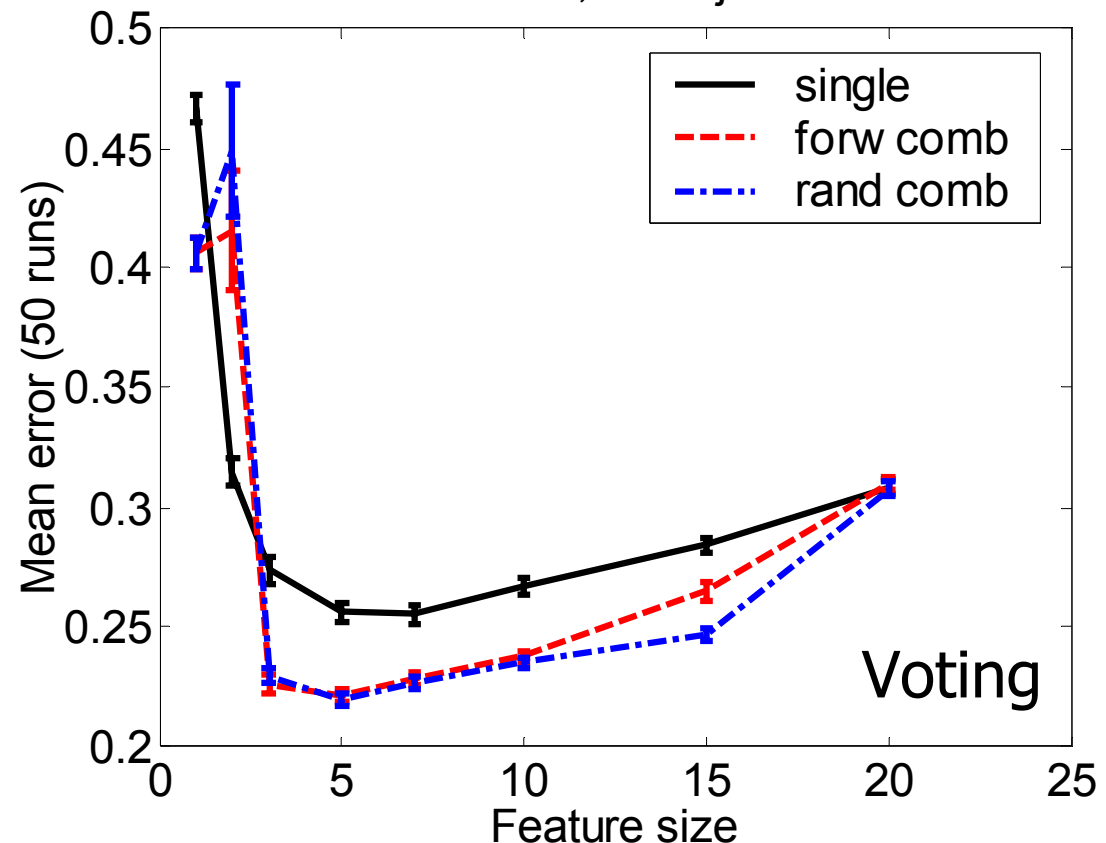
Features: 34

Satellite, 60 objects



Weighted Voting

Satellite, 60 objects



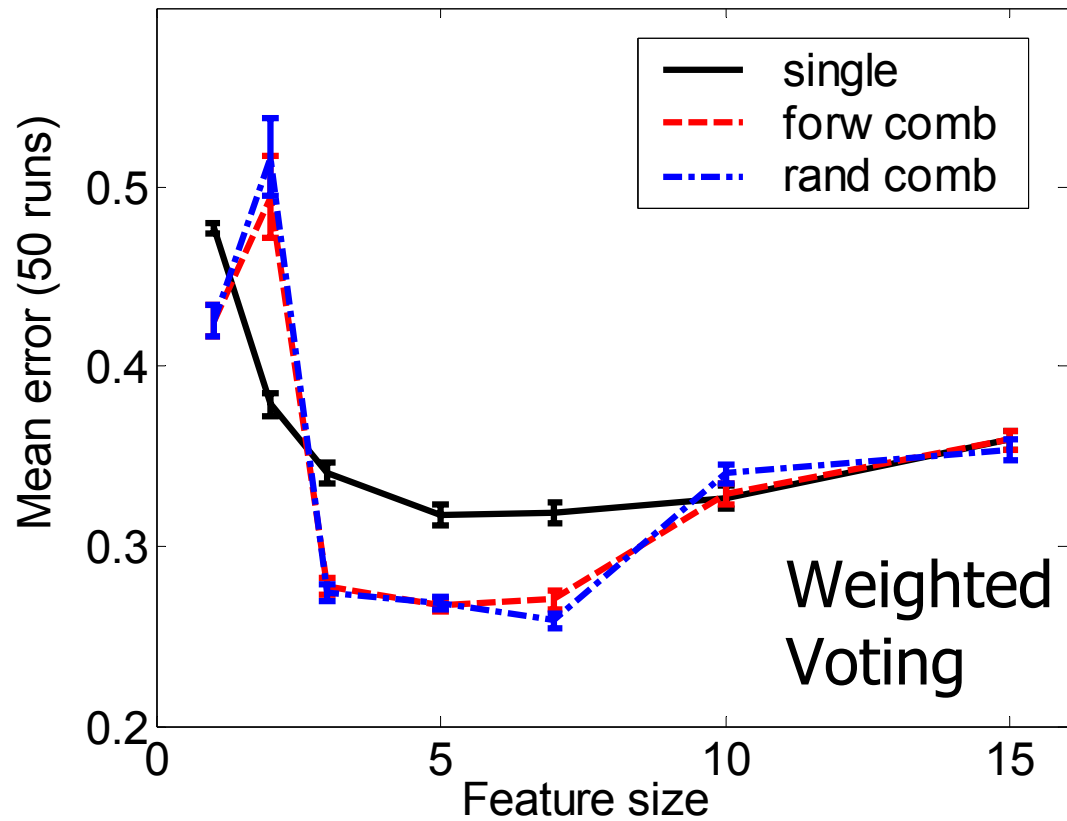
Voting

Objects: 6435 (1533+703+1358+626+707+1508)

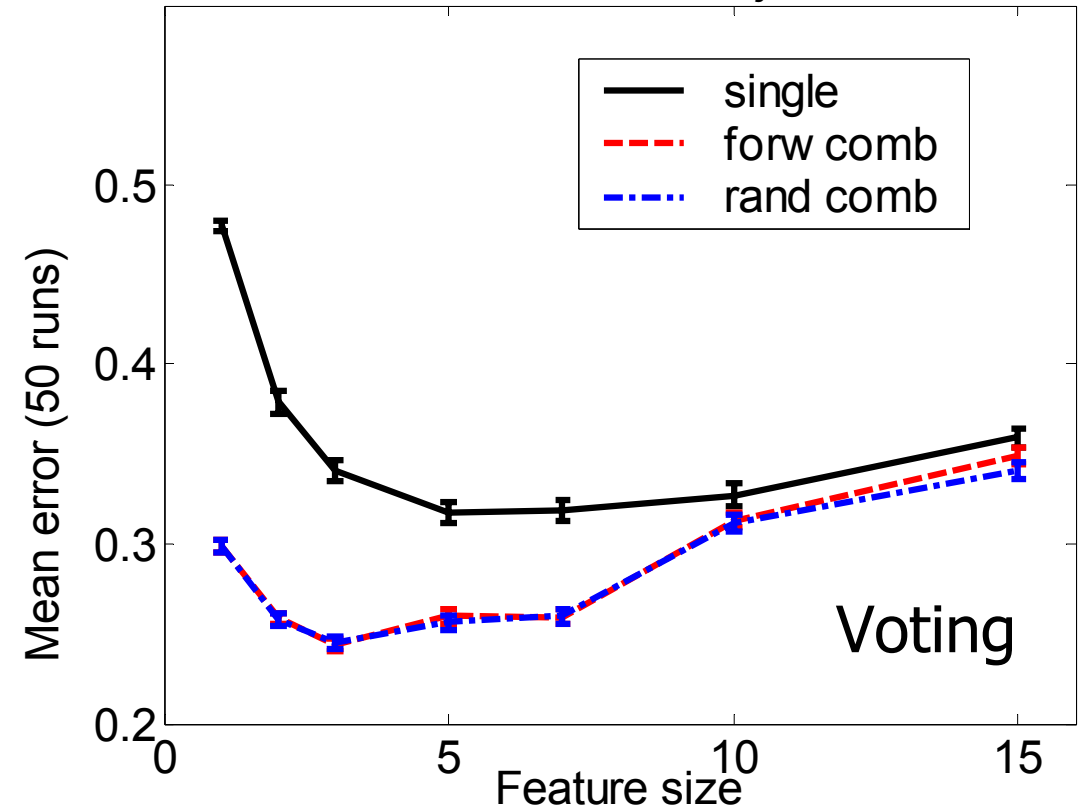
Features: 36

Waveform

Waveform, 45 objects



Waveform-v, 45 objects

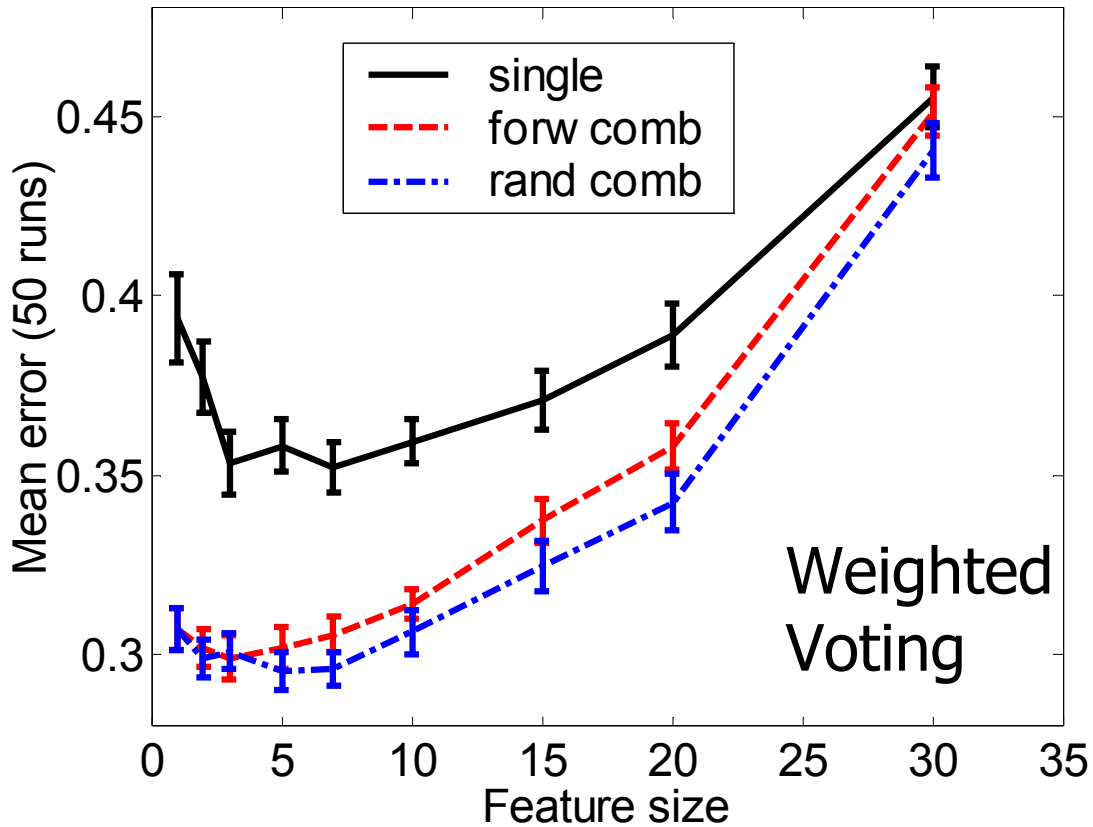


Objects: 5000 (1657+1647+1696)

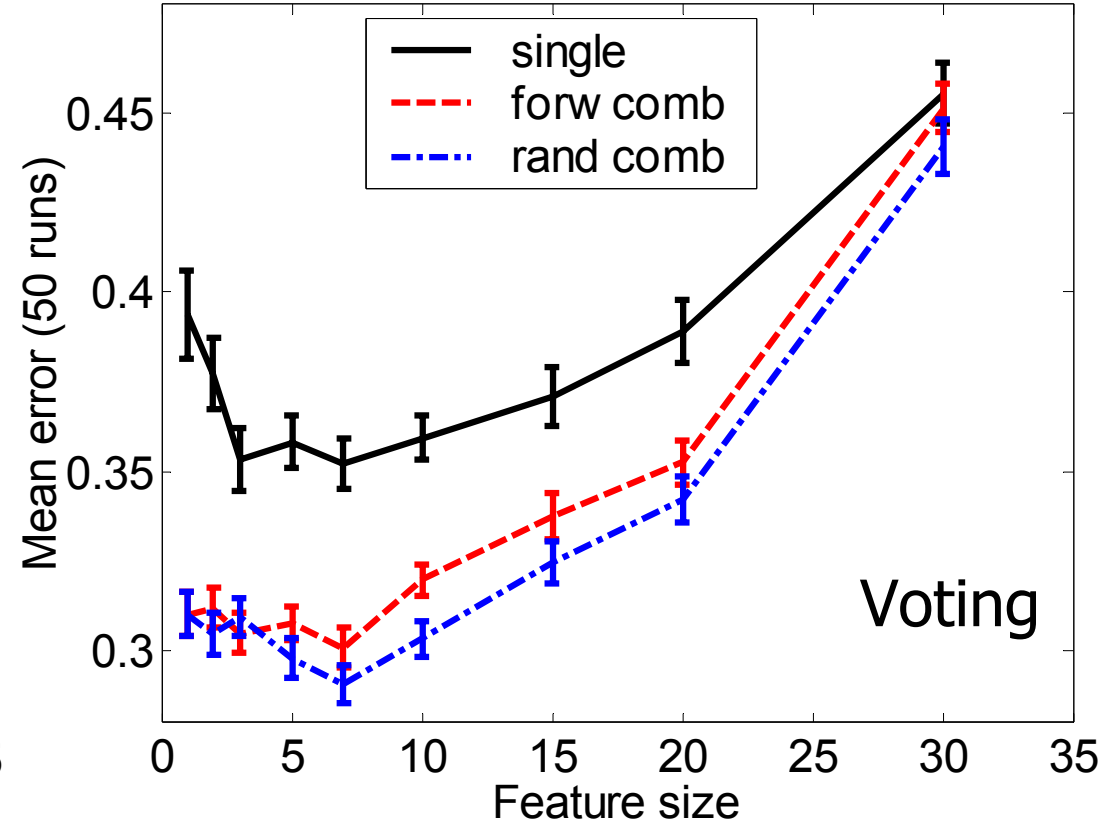
Features: 21

Sonar

Sonar, 30 objects



Sonar-v, 30 objects

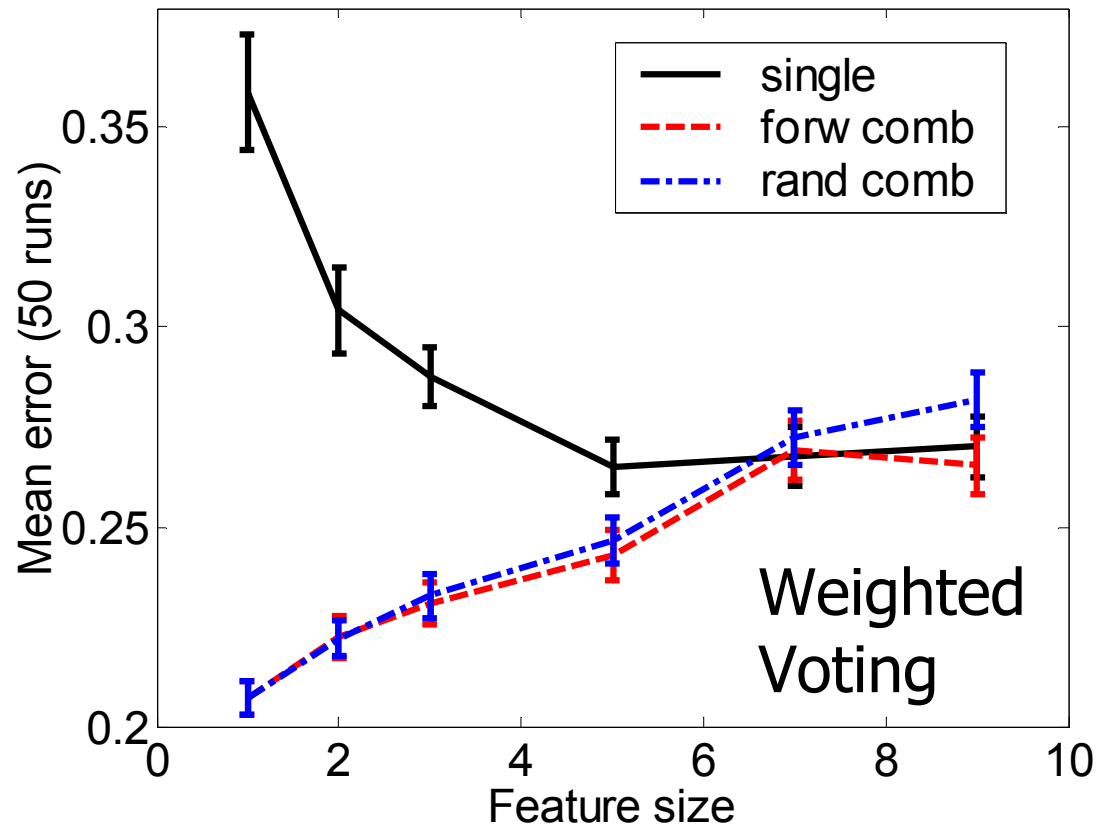


Objects: 208 (97+11)

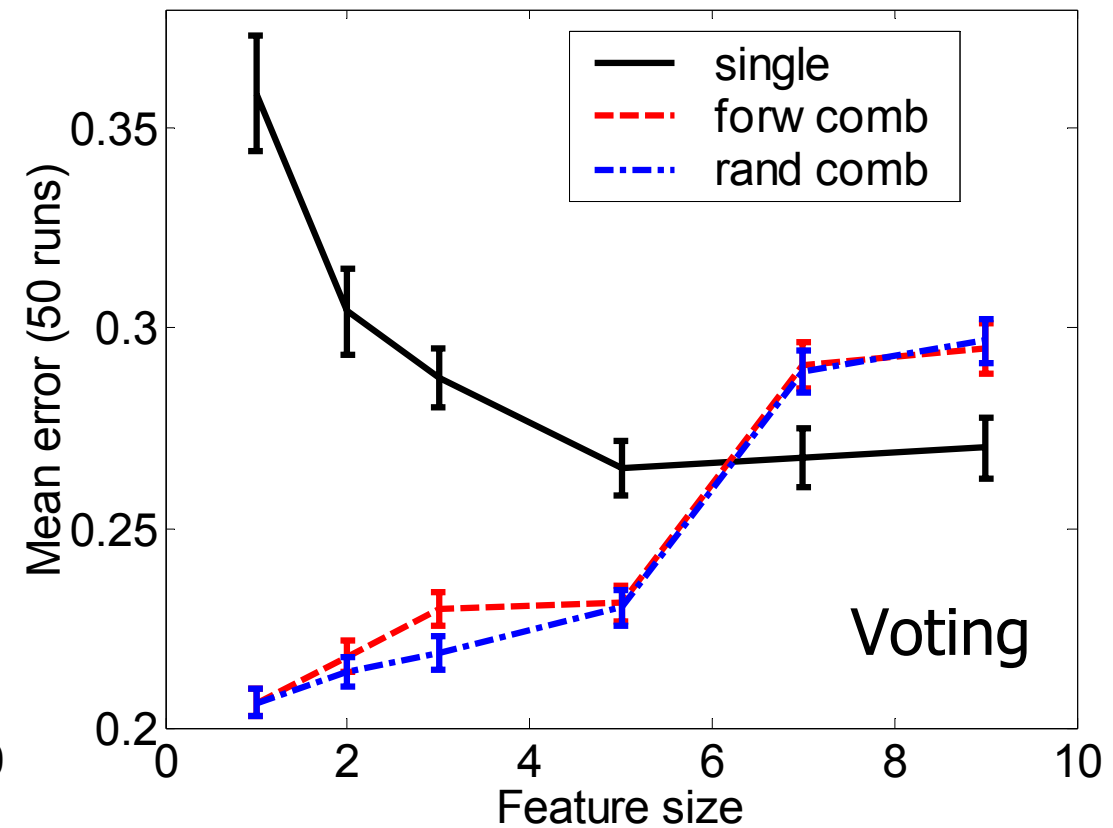
Features: 60

Heart Dataset

Heart, 20 objects



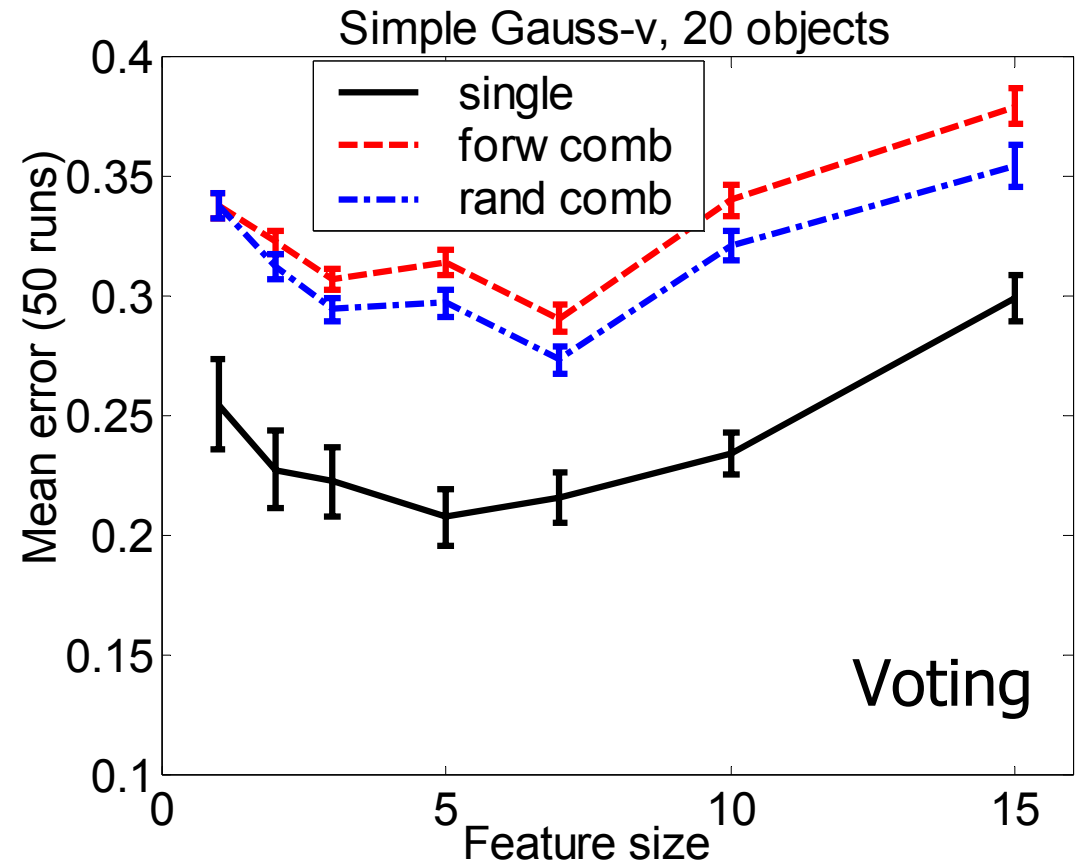
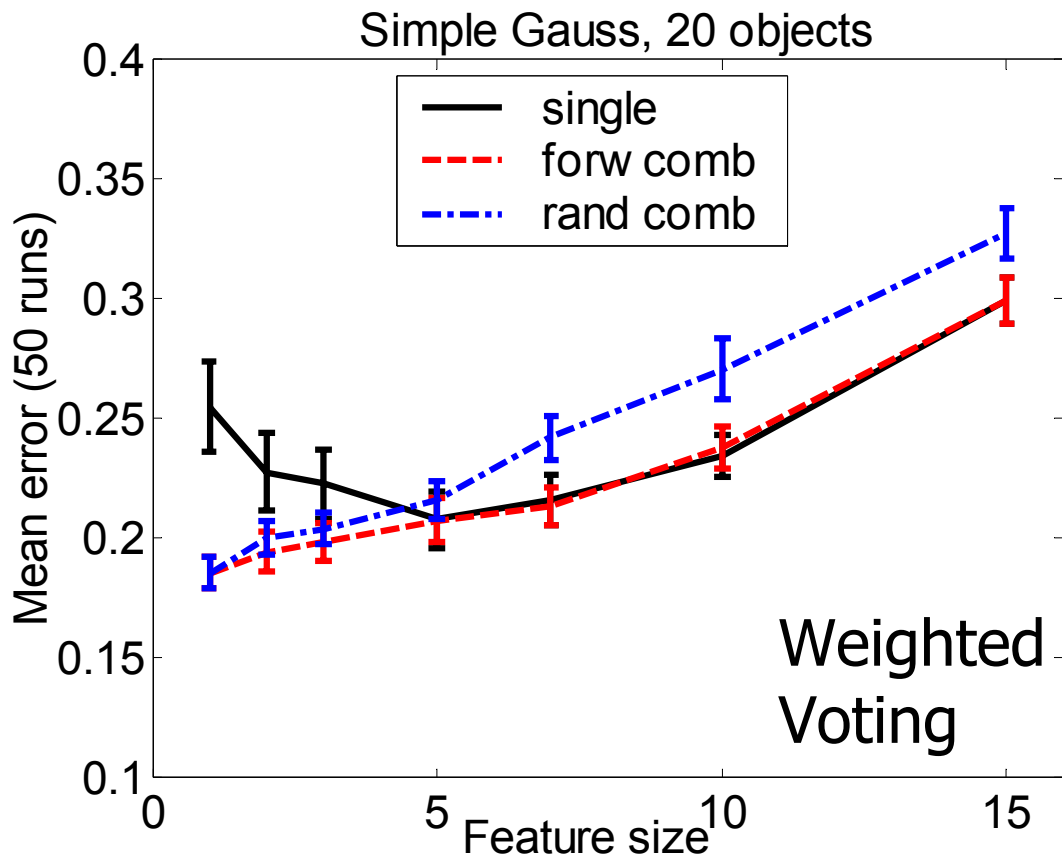
Heart-v, 20 objects



Objects: 297 (160+137)

Features: 13

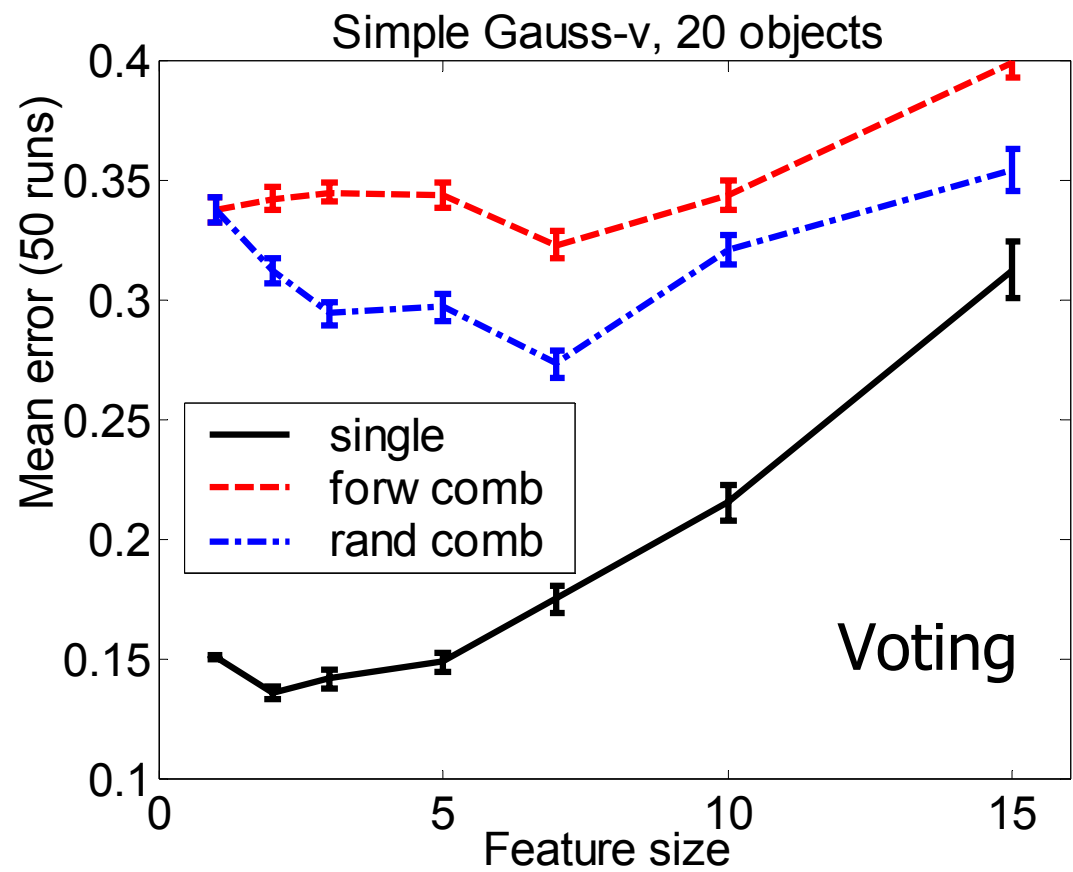
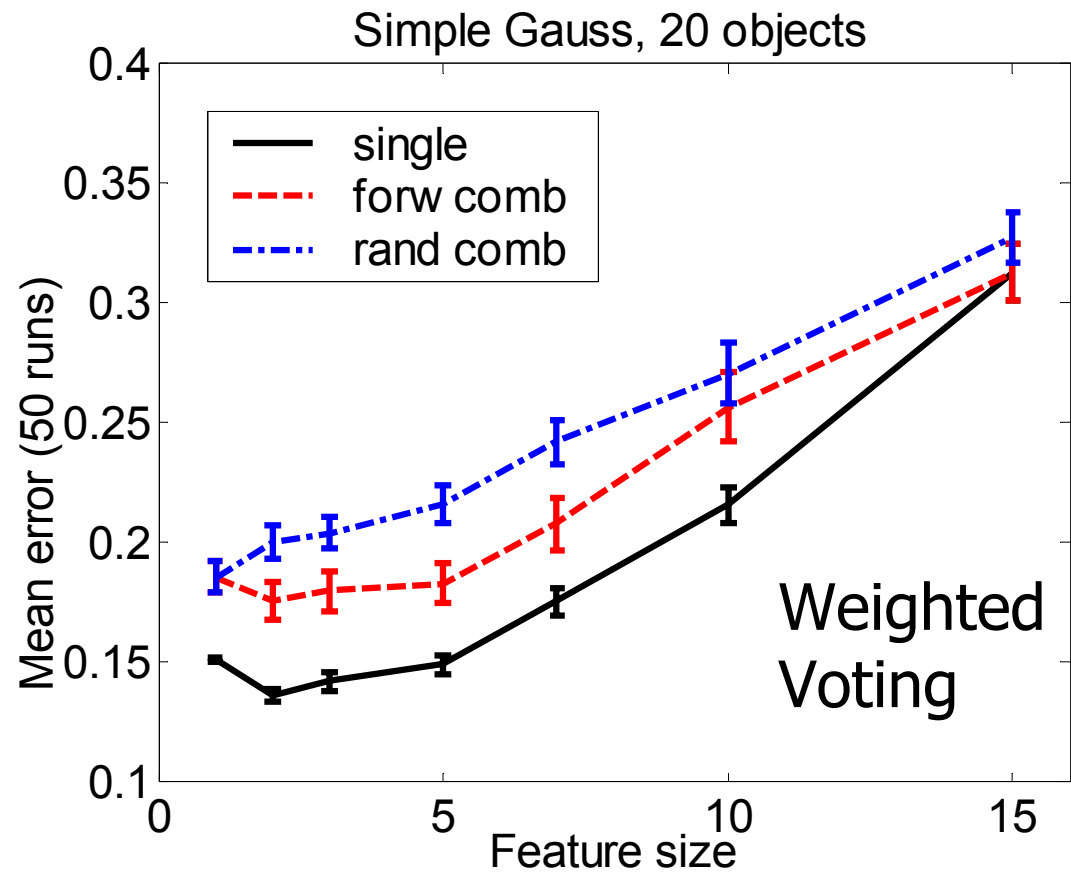
Simple Gauss, No Feature Selection



Objects: 500 (250+250)

Features: 20, $d = 2 / n$, $n = 1, 20$

Simple Gauss, Optimal Feature Order



Objects: 500 (250+250)

Features: 20, $d = 2 / n$, $n = 1, 20$

Conclusions

- Feature selection may be improved by a combined subspace approach based on all features.
- This approach does not deteriorate the result.
- Random feature ordering might do equally well.

Conclusions

- Feature selection may be improved by a combined subspace approach based on all features.
- This approach does not deteriorate the result.
- Random feature ordering might do equally well.
- The procedure may not work for an initially well ranked set of features